

Building Useful Factors and Scales to Aid in the Assessment of Learning Gains and Other Student Outcomes

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This presentation

- General factor analysis overview
- Example of creating and refining a factor
- Use of factor score in comparing institutions
- Use of factor score in examining student experiences and outcomes
- Future directions for research at CIRP



What is Factor Analysis?

- Mathematical procedure to analyze interrelationships (correlations) among a set of variables
- Can explain the interrelationships in terms of a reduced number of variables – factors
 - Factors: hypothetical (latent) variables that influence scores on one or more observed variables
 - Factors represent the "reason" why variables are highly correlated



Two Kinds of Factor Analysis

Exploratory Factor Analysis (EFA)

 Explore the underlying structure of a set of observed variables without imposing a preconceived structure on the outcome

Confirmatory Factor Analysis (CFA)

- Allows the researcher to test whether a hypothesized relationship between observed variables and their underlying latent construct(s) exists. The relationship is postulated a priori and then tested statistically.
- Both analyses tell us whether the responses to a set of survey questions are organized into clusters, but have different functions

Exploratory Factor Analysis Example: Cross-Racial Interactions (YFCY)

13. To what extent have you experienced the following with students from a racial/ethnic group <u>other than your own</u>? (Mark one for each item)

	'Y Othou	ten ten	metimo	ldom	Ver
	S	ð	S	S	Ne Ne
Dined or shared a meal	\bigcirc	\bigcirc	0	0	\bigcirc
Had meaningful and honest discussions					
about race/ethnic relations outside of class .	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
Had guarded, cautious interactions	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
Shared personal feelings and problems	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
Had tense, somewhat hostile interactions	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
Had intellectual discussions outside of class	\bigcirc	\bigcirc	0	\bigcirc	\bigcirc
Felt insulted or threatened because of					
race/ethnicity	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
Studied or prepared for class	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
Socialized or partied	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc
Attended events sponsored by other					
racial/ethnic groups	\bigcirc	\bigcirc	\bigcirc	\bigcirc	\bigcirc



Correlation Matrix

	1	2	3	4	5	6	7	8	9	10
1 Dined or shared a meal	1									
2 Discussed race/ethnic relations outside class	0.61	1								
3 Had guarded, cautious interactions	0.25	0.40	1							
4 Shared personal feelings and problems	0.65	0.63	0.29	1						
5 Had tense, somewhat hostile interactions	0.18	0.31	0.59	0.26	1					
6 Had intellectual discussions outside of class	0.63	0.66	0.27	0.72	0.25	1				
7 Felt insulted or threatened because of race/ethnicity	0.12	0.25	0.50	0.16	0.62	0.16	1			
8 Studied or prepared for class	0.56	0.52	0.28	0.61	0.27	0.65	0.17	1		
9 Socialized or partied	0.60	0.49	0.19	0.60	0.18	0.57	0.11	0.55	1	
10 Attended events by other racial/ethnic groups	0.45	0.50	0.28	0.46	0.26	0.47	0.26	0.47	0.48	1



Exploratory Factor Analysis

Three stages:

- (1) choose an extraction method
- (2) decide the number of factors
- (3) choose a rotation method



Extraction

- Two common extraction techniques:
 - Component (In SPSS: Principal Components Analysis, PCA)
 - A data reduction method
 - Utilizes all of the variance in a set of variables
 - Most common
 - "True" Factor analysis (In SPSS: Principal Axis Factoring, PAF)
 - Also a data reduction method, but assumes that the variables co-vary in some way
 - Uses only the shared variance (correlations) of a set of variables to compute the factor solution
- Some researchers prefer one method, some prefer the other.
 - Many researchers believe that Principal Components Analysis is not appropriate for exploratory factor analysis



Number of Factors: How to decide?

- Choose a set of variables
- Run a factor analysis using extraction method chosen
 - Here: Principal Axis Factoring
- Examine Scree Plot
 - Plots Eigenvalues of all possible factors



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Rotation

- Rotation simplifies and clarifies the underlying data structure
- Two common rotation methods:
 - Varimax orthogonal rotation that assumes uncorrelated factors
 - Produces cleaner and more easily interpreted results
 - May not be appropriate for "messy" data of the real world
 - Promax Oblique rotation method that allows factors to correlate
 - Produces slightly more complex output to interpret
 - May more accurately resemble the "real world"
- If factors are truly uncorrelated, both rotations will produce nearly identical results

Output from both rotational methods

PAF, Varimax

Rotated Factor Matrix

	Factor							
	1	2						
Had intellectual discussions outside of class	.825	.141						
Shared personal feelings and problems	.816	.151						
Dined or shared a meal	.783	.086						
Socialized or partied	.724	.066						
Studied or prepared for class	.723	.170						
Had meaningful and honest discussions about race/ethnic relations outside of class	.716	.283						
Attended events sponsored by other racial/ethnic groups	.564	.245						
Had tense, somewhat hostile interactions	.151	.822						
Felt insulted or threatened because of race/ethnicity	.076	.731						
Had guarded, cautious interactions	.231	.673						

Extraction Method: Principal Axis Factoring. Rotation Method: Varimax with Kaiser Normalization. PAF, Promax

Pattern Matrix ^a								
	Factor							
	1	2						
Had intellectual discussions outside of class	.848	030						
Shared personal feelings and problems	.837	018						
Dined or shared a meal	.815	079						
Socialized or partied	.757	087						
Studied or prepared for class	.734	.023						
Had meaningful and honest discussions about race/ethnic relations outside of class	.702	.145						
Attended events sponsored by other racial/ethnic groups	.548	.138						
Had tense, somewhat hostile interactions	014	.841						
Felt insulted or threatened because of race/ethnicity	075	.761						
Had guarded, cautious interactions	.103	.665						

Extraction Method: Principal Axis Factoring. Rotation Method: Promax with Kaiser Normalization.

a. Rotation converged in 3 iterations.

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a. Rotation converged in 3 iterations.



Evaluating the fit of items in a factor Cronbach's Alpha Commonalities

Reliability Statistics

Cro	onbach's		Item-Tota	I Statistics		
E	Alpha N of Items .901 7		Scale Mean if Item Deleted	Scale Variance if Item Deleted	Corrected Item-Total Correlation	Cronbach's Alpha if Item Deleted
	Dined or shared a meal		17.64	37.177	.735	.884
	Had meaningful and honest discussions about race/ethnic relations outside of class	ut	18.30	37.476	.711	.886
	Shared personal feeling and problems	S	18.04	36.518	.775	.879
	Had intellectual discussions outside of class		18.05	36.493	.783	.878
	Studied or prepared for class		18.04	36.900	.701	.888
	Socialized or partied		17.83	37.885	.684	.889
	Attended events sponsored by other racial/ethnic groups		18.67	39.581	.574	.901

Communalities

	Initial	Extraction
Dined or shared a meal	.562	.621
Had meaningful and honest discussions about race/ethnic relations outside of class	.569	.593
Had guarded, cautious interactions	.427	.506
Shared personal feelings and problems	.630	.689
Had tense, somewhat hostile interactions	.504	.699
Had intellectual discussions outside of class	.647	.700
Felt insulted or threatened because of race/ethnicity	.421	.541
Studied or prepared for class	.514	.552
Socialized or partied	.492	.529
Attended events sponsored by other racial/ethnic groups	.366	.378
Extraction Method: Principal	Axis Factori	ng.



Creating Factor Scores

- Factor score score that theoretically would have been obtained for a person had we been able to measure the latent factor directly
- Coarse Factor Scores unweighted composites (averages or sums) of the items having salient factor loadings
- Refined Factor Scores use information from the correlation matrix or factor coefficients to weight the combination of items
 - Ex. Thurstone's least squares regression approach (in SPSS, "Regression,")
- Generally, researchers agree that refined scores have less bias than coarse scores
 - However, weights are sample-dependent
 - Refined scores are best option if one wants to employ a weighting scheme that uses all of the items (not just the items that load on one factor)



Using Factor Scores For Institutional Assessment

- Computed Regression Estimates from SPSS for Positive Racial/Ethnic Relations Factor
 - Mean =0, Standard Deviation \approx 1
- Can compare any institution or group of institutions on their scores
- Examples to follow that use the 2008 Your First College Year (YFCY) data
 - 501 institutions; 41,118 students
 - California: 33 institutions; 4,273 students
 - New York: 57 institutions; 3,325 students



Comparing Levels of Positive Racial/Ethnic Interaction: By State



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Comparing Levels of Positive Racial/ Ethnic Interaction: By State & Gender



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What leads to positive racial/ethnic interaction?

Use the factor score as the dependent variable in a regression

	Coefficients ^a								
		Unstandardized Coefficients		Standardized Coefficients					
Model		В	Std. Error	Beta	t	Sig.			
1	(Constant)	-1.185	.036		-33.209	.000			
	That your courses inspired you to think in new ways	.207	.008	.138	27.489	.000			
	Performed volunteer work	.127	.008	.089	16.930	.000			
	Participated in student government	.168	.017	.050	9.938	.000			
	Joined a social fraternity or sorority	039	.015	013	-2.565	.010			
	Participated in student clubs/groups	.212	.010	.108	20.508	.000			
	Enrolled in a formal program where a group of students take two or more courses together (e.g., FIG, learning cluster, learning community, linked courses)	.067	.014	.024	4.933	.000			
	Your sex (Male)	038	.010	019	-3.834	.000			

a. Dependent Variable: Positive Racial/Ethnic Relations



Does positive racial/ethnic interaction lead to positive student outcomes?

Use the factor score as an independent variable in a regression

	Coefficients ^a								
		Unstandardized Coefficients		Standardized Coefficients					
Model		В	Std. Error	Beta	t	Sig.			
1	(Constant)	2.780	.024		117.390	.000			
	HPW past year: Studying/homework	.051	.002	.104	20.813	.000			
	HPW past year: Talking with professors outside of class	.040	.004	.055	11.021	.000			
	The Faculty here are interested in students' academic problems (Agreement)	.170	.005	.158	31.132	.000			
	Easy to understand what your professors expect of you academically?	.043	.006	.043	7.628	.000			
	Easy to develop effective study skills?	.053	.005	.060	10.983	.000			
	Positive Racial/Ethnic Relations	.053	.004	.074	15.005	.000			

a. Dependent Variable: Critical thinking skills



Additional Considerations

- Reliability results stable over time?
- Validity measure what we think it does?
- Same factor structure for different groups?
- What to do when combining items with different scales?
 - Standardize items?
 - Item Response Theory (IRT) a more methodologically sophisticated way to construct scales representing latent traits



Current projects at CIRP

- Methodological examination of factor score computation
- Methodological investigation into IRT
 - Advantages and disadvantages over "classic" factor analysis for the creation of scales from college student surveys
- Creation of database of factors that have been used in published research
 - Easy to apply at your institution



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